



ORIGINAL ARTICLE

Calculation method for the dielectric constant of thioglycolic acid grafted modified SBS dielectric elastomer



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Connectivity index;
Dipole moment fluctuation

Abstract Nonpolar/polar block copolymer materials can be used to develop high-performance dielectric elastomer materials. At present, there is no method to accurately predict its dielectric constant, which is not conducive to improving related research and development efficiency. For this, styrene-butadienestyrene triblock copolymer (SBS) block copolymer grafted modified by thioglycolic acid (TGA) is chosen as the research object. We propose a hybrid calculation method combining the group contribution method, the connectivity index method, and the dipole moment fluctuation method. The connectivity index method and the dipole moment fluctuation method calculate the dielectric constants of nonpolar and polar repeat units to provide accurate basic data for the group contribution method. In the calculation process, the Vogel model completes the mutual conversion between dielectric constant and molar polarizability. Both theoretical calculation and experimental verification show that the dielectric constant of SBS-TGA increases with the grafting rate. We found the correlation between theoretical calculations and experimental values and confirmed that the applicable frequency range of this method is 1 kHz–1000 kHz. This method can be extended to predict the dielectric constant of other polymers and improve development efficiency.

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1. Introduction

Dielectric Elastomer (DE) has a large strain, high energy density, and fast response speed. It has crucial application potential in flexible electronic equipment such as artificial muscles, implantable biological electronic devices, micro energy harvesting, sensors, etc. (Brochu and Pei, 2010; Madsen et al., 2016a,b; Pelrine et al., 2000).

From Eq. (1) for evaluating the electromechanical properties of the material, it can be seen that the dielectric constant

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is one of the essential factors that determine the properties of DE materials (Pelrine et al., 1998; Molberg et al., 2009; Kussmaul et al., 2011). For DE materials with the same Young's modulus, the greater the dielectric constant, the stronger the energy conversion ability (Koh et al., 2009; Lv et al., 2015; Han et al., 2020).

$$S_z = P/Y = -\varepsilon_0 \varepsilon_r E^2 / Y \quad (1)$$

where S_z is the strain in the thickness direction of the DE material under the action of the electric field, Y is the elastic modulus of the material, P is the Maxwell force, ε_0 is the vacuum dielectric constant, ε_r is the relative dielectric constant, and E is electric field strength acting on the material.

At present, modified or synthesized block copolymers are often used to develop high-performance dielectric elastomer materials (Chen et al., 2021; Ma et al., 2017; Tian et al., 2016; Zhao et al., 2018a,b). For example, the overall electromechanical performance of modified SBS has been significantly improved after being grafted and modified with polar groups, such as thioglycolic acid and methyl thioglycolate (Gress et al., 2007; Sun et al., 2016; Ellingford et al., 2018). Screening suitable polar groups are of great significance to the development of new SBS-based dielectric elastomers. The traditional "synthesis then test" screening method is time-consuming and costly. Computer-aided calculation of the dielectric constant of modified SBS can improve the efficiency of research and development (Frühbeis et al., 1987; Satyanarayana et al., 2009; Holtje, 2011), such as group contribution (GC) method, connectivity index (CI) method, and dipole moment fluctuation (DMF) method.

GC method is a classic structure–property analysis method (Vankrevelen and Hoftyzer, 1969; Martin, 1981). In recent years, there are still developments and applications in refractive index (Gharagheizi et al., 2014), heat capacity (Walker and Haslam, 2020), atmospheric lifetime (Eini et al., 2020), etc. The same group shows the same contribution to certain characteristics of different molecules is the theoretical basis of this method (Vankrevelen and Hoftyzer, 1969; Krevelen, 1990; Bicerano, 1992). The polymer molecular chain is divided into different repeating units, and the dielectric constant of the polymer can be accurately calculated according to the contribution value of each repeating unit (Bicerano, 2002; Zhou et al., 2014). Gladstone-Dale model (Gladstone and Dale, 1858), Lorentz-Lorenz model (Lorenz, 1880; Ha, 1880; Zhou et al., 2014), Vogel model (Vogel, 1948), etc., as shown in Eqs. (2)–(4) are often used. The first two models have a good theoretical explanation, and the Vogel model is a simple empirical formula. The three models have the same standard deviation (Van Krevelen Willem and Nijenhuis, 1976). This method cannot be used without the group contribution value of any repeating unit, and the need for complete experimental data as support is its obvious disadvantage (Katritzky et al., 1998).

$$\varepsilon = \left(1 + \frac{P_{GD}}{V}\right)^2 \quad (2)$$

$$\varepsilon = \frac{V + 2P_{LL}}{V - P_{LL}} \quad (3)$$

$$\varepsilon = \left(\frac{P_V}{M}\right)^2 \quad (4)$$

where ε is the dielectric constant, V is the molar volume of the molecule, P_{LL} , P_{GD} , and P_V respectively represent the molar polarizability of the molecule in the Lorentz-Lorenz, Gladstone-Dale, and Vogel models, and M represents the molar mass of the molecule.

The CI method is a structure–property analysis method developed based on chemical graph theory (Kier and Hall, 1976a,b, 1986). In recent years, there are still developments and applications in the carcinogenicity prediction of substances (Li et al., 2019), drug agonistic activity analysis (Raghuraj et al., 2020), and quantitative structure–activity relationship modeling (Zakharov et al., 2019; Song et al., 2020). The principle is the correlation between the connectivity index calculated accurately based on the valence bond structure and the properties of interest (Kier and Hall, 1976a,b, 1986). The CI method is simple to calculate and does not require experimental data support, and can accurately predict the permittivity of many nonpolar polymers (Polak and Sundahl, 1989; Camarda and Maranas, 1999). The applicable frequency range of the CI method is optical frequency, and the only induced polarization of nonpolar polymers under the action of an electric field occurs in this frequency range (Mossotti, 1847), so the connectivity index can be used to calculate the dielectric constant (Kier and Hall, 1976a,b, 1986) accurately. However, under the action of an electric field, polar molecules have two processes of induced polarization and orientation polarization. Their molecular polarization is shown in Eq. (5) (Mossotti, 1847), and the relationship between molecular polarization and dielectric constant is shown in Eq. (6) (Clausius, 1879; Böttcher, 1973). The frequency range corresponding to orientation polarization is lower, making the CI method unable to calculate the dielectric constant of polar molecules accurately.

$$\alpha = \alpha_d + \alpha_\mu = \alpha_d + \frac{\mu_0^2}{3k_B T} \quad (5)$$

$$\frac{\varepsilon - 1}{\varepsilon + 2} = \frac{N_0 \alpha}{3\varepsilon_0} \quad (6)$$

where ε is the dielectric constant of the molecule, N_0 is the number of molecules per unit volume, α is the molecular polarizability, ε_0 is the vacuum dielectric constant, α_d is the induced polarizability, α_μ is the orientation polarizability, μ_0 is the permanent dipole moment, k_B is Boltzmann's constant, and T is the thermodynamic temperature.

The DMF method is a calculation method of dielectric properties based on molecular dynamics (Williams, 1972; De Leeuw et al., 1980; Neumann, 1983; Adams and Adams, 2006). In recent years, there still are developments and applications in the analysis of the permittivity of supercritical water (Hou et al., 2020) and organic semiconductors (Sami et al., 2020), and the analysis of dielectric relaxation of crystals (Mattoni and Caddeo, 2020). The calculation principle is the relationship between the dipole moment–time correlation function and the macroscopic complex permittivity derived from molecular theory (Williams, 1972). At present, the research objects of the DMF method are mainly small molecules and low polymerization degree polymers (Anderson et al., 1987; Skaf, 1997; Smith et al., 2002). The DMF method is often used in the analysis of material induce polarization, but the commonly used fixed force field (Jorgensen et al., 1996; Chen and Siepmann, 1999; Huang et al., 2017) is not effective in dealing

with the dielectric constant calculation of nonpolar molecules, such as benzene. The value and the experimental values are 1.005 (Cardona et al., 2020) and 2.25 (Mardolcar et al., 1992), respectively. The orientation polarizability that dominates the molecular polarizability of polar materials can be accurately estimated by molecular dynamics (Cardona et al., 2020). Therefore, the DMF method to calculate the dielectric constant is mainly suitable for small molecule polar systems (Neumann, 1983; Anderson et al., 1987; Skaf, 1997).

The SBS molecular chain modified by polar groups contains both nonpolar and polar repeating units. The complementary advantages of the CI method and DMF method can accurately calculate the dielectric constant of all repeating units. Therefore, this paper uses the CI method and DMF method to calculate the dielectric constants of nonpolar and polar repeating units, respectively, to provide accurate basic data for the GC method, and form a hybrid calculation method suitable for the calculation of the dielectric constant of grafted modified SBS. The theoretical calculation of SBS-TGA is consistent with the experimental measurement results, and the deviation between the two can be corrected by adjusting the fitting parameters.

2. Calculation method

2.1. Division of repeating units

Many synthetic macromolecular materials have relatively simple structures, and identical structures that recur in the molecular chain are defined as repeating units. If the repeating units are the same, the material is a homopolymer. If there are more than two repeating units, the material is a copolymer. Polymer molecular chains consist of a “backbone” and peripheral atoms or groups. The end groups in finite-size polymer chains are not repeating units and have little effect on the physical properties and are usually not considered.

The polymer molecular chain is divided into repeating units by searching for recurring identical structures along with the polymer skeleton. For subsequent analysis, the repeating units containing polar functional groups such as carboxylic acids, alcohols, amides, thiols, and ketones are classified as polar groups. Those containing only nonpolar functional groups such as alkanes and alkenes are classified as nonpolar groups.

The molecular structure of SBS-TGA is shown in Fig. 1a and can be divided into six repeating units, St, Cis-1,4-Bu, Trans-1,4-Bu, 1,2-Bu, 1,4-Bu-TGA, and 1,2-Bu-TGA (Segre et al., 1975; Kussmaul et al., 2011), denoted by G_1, G_2, \dots, G_6 , respectively, as shown in Fig. 1b. G_1, G_2, G_3 , and G_4 are classified as nonpolar sets, and G_5 and G_6 are classified as polar sets.

2.2. Calculation of dielectric constant of the nonpolar repeating unit

2.2.1. Calculation of connectivity index

For the nonpolar repeating unit G_i , the dielectric constant ϵ_i is calculated using the CI method. First, the hydrogen-suppressed graph is constructed from the valence bond diagram of the repeating unit, as shown in Fig. 2a and Fig. 2b, taking G_1 as an example.

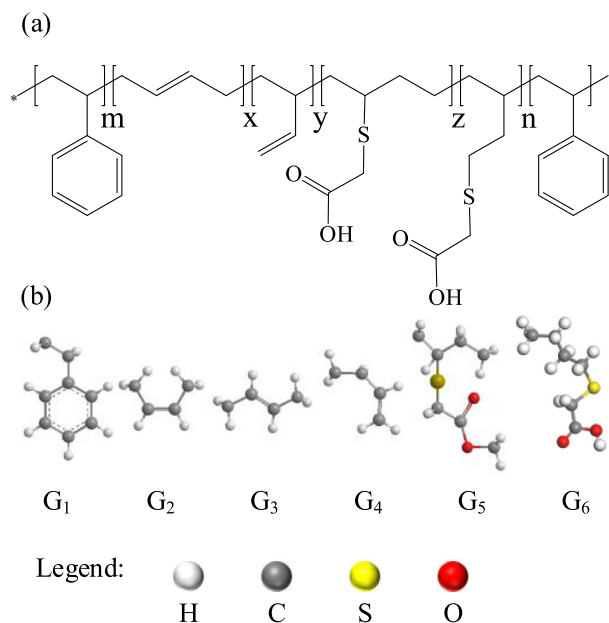


Fig. 1 (a) The molecular structure of SBS-TGA, (b) the repeating units G_1 - G_6 : St, Cis-1,4-Bu, Trans-1,4-Bu, 1,2-Bu, 1,4-Bu-TGA, 1,2-Bu-TGA.

The atomic indices δ and δ^V describe the electronic environment and the bond configuration of each non-hydrogen atom in the molecule. δ is the simple connectivity index and is equal to the number of edges emanating from that vertex in the hidden hydrogen diagram. δ^V is the valence connectivity index and is defined by Eq. (7) (Randic, 2015). The calculation

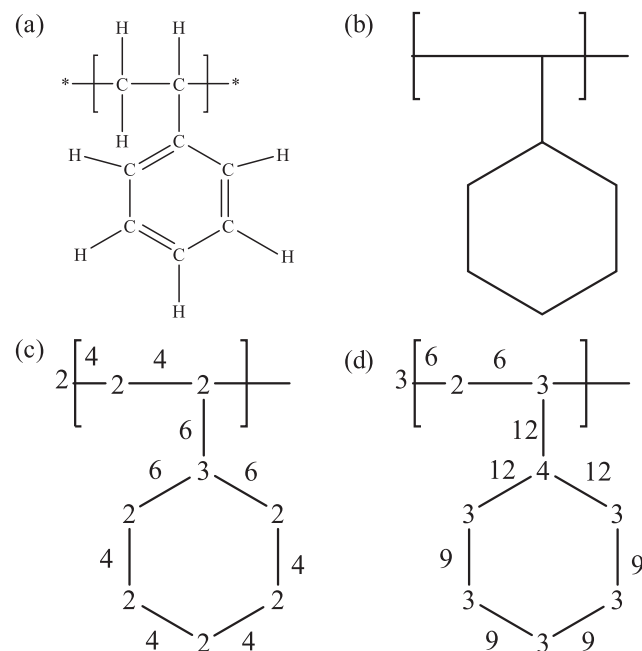


Fig. 2 (a) The valence-bond structure of G_1 , (b) The hydrogen-suppressed graph of G_1 ; (c) The δ value on the vertex and the β value on the edge; (d) The δ^V value on the vertex and the β^V value on the edge.

results are shown in Fig. 2c and the values at the vertices in Fig. 2d.

$$\delta^V = \frac{Z^V - N^H}{Z - Z^V - 1} \quad (7)$$

where Z^V is the number of valence electrons of the atom, N_H is the number of hydrogen atoms bonded to it, and Z is its atomic number.

The value corresponding to each bond that does not involve a hydrogen atom is defined as the bond index, and the bond index β and β^V are determined by the product of the atomic indices (δ and δ^V) at the two vertices (i and j) connected by the edges, as shown in Eqs. (8) and (9). Taking G_1 as an example, the calculation results are marked on the edges of the hydrogen-suppressed graph in Fig. 2c and Fig. 2d

$$\beta_{ij} = \delta_i \cdot \delta_j \quad (8)$$

$$\beta_{ij}^V = \delta_i^V \cdot \delta_j^V \quad (9)$$

The zero-order connectivity index (${}^0\chi$, ${}^0\chi^V$) of the whole molecule and is defined based on the atomic index of all vertices of the hydrogen-suppressed graph, as shown in Eqs. (10) and (11) (Randic, 1975). Taking G_1 as an example, the results are calculated as 5.397 and 4.671, respectively.

$${}^0\chi = \sum_{\text{vertices}} \left(\frac{1}{\sqrt{\delta}} \right) \quad (10)$$

$${}^0\chi^V = \sum_{\text{vertices}} \left(\frac{1}{\sqrt{\delta^V}} \right) \quad (11)$$

The first-order connectivity index (${}^1\chi$, ${}^1\chi^V$) of the whole molecule is defined based on the bond index on all edges of the hydrogen-suppressed graph, as shown in Eqs. (12) and (13) (Randic, 1975). Taking G_1 as an example, the results are calculated as 3.966 and 3.015, respectively.

$${}^1\chi = \sum_{\text{edges}} \left(\frac{1}{\sqrt{\beta}} \right) \quad (12)$$

$${}^1\chi^V = \sum_{\text{edges}} \left(\frac{1}{\sqrt{\beta^V}} \right) \quad (13)$$

The zero-order and first-order connectivity indexes of G_1 – G_4 are shown in Table 1. For computational simplicity, this paper does not use higher-order connectivity indexes (Kier and Hall, 1976a,b), and various types of structural parameters are used to supplement the zero- and first-order connectivity indexes.

2.2.2. Calculation of dielectric constant

Based on the study of Darby, J R et al. (Darby et al., 1967), Bicerano proposed an improved metric method for calculating the dielectric constant of nonpolar repetitive cells (Bicerano, 2002), as shown in Eq. (14).

Table 1 Zero-order and first-order connectivity index.

Repeating units	${}^0\chi$	${}^0\chi^V$	${}^1\chi$	${}^1\chi^V$
G_1	5.397	4.671	3.966	3.015
G_2	2.828	2.568	2.000	1.649
G_3	2.828	2.568	2.000	1.649
G_4	2.991	2.568	1.931	1.558

$$\varepsilon_{(298K)} \approx \frac{0.001887E_{coh1} + N_{dc}}{V_W} + 1.412014 \quad (14)$$

where E_{coh1} is the cohesion energy expressed in terms of the first-order connectivity index (Darby et al., 1967), as shown in Eqs. (15)–(17), N_{dc} is the structure correction parameter for the dielectric constant, and V_W is the van der Waals volume (Bondi, 1964), which is calculated as shown in Eqs. (19)–(20). The unit of E_{coh1} is kJ/mol, N_{dc} is a constant, and the unit of V_W is cm^3/mol .

$$E_{coh1} \approx 358.7(6N_{\text{atomic}} + 5N_{\text{group}}) + 9882.5^1\chi \quad (15)$$

where N_{atomic} is the atomic correction term, and N_{group} is the group correction term.

$$N_{\text{atomic}} = 4N_{(-S-)} + 12N_{\text{sulfone}} - N_F + 3N_{Cl} + 5N_{Br} + 7N_{\text{cyanide}} \quad (16)$$

where $N_{(-S-)}$ is the number of sulfur atoms in the divalent oxidation state, N_{sulfone} is the number of sulfur atoms in the highest oxidation state, N_F , N_{Cl} , and N_{Br} is the number of fluorine, chlorine, and bromine atoms, respectively, and N_{cyanide} is the number of nitrogen atoms at $\delta = 1$ and $\delta^V = 5$.

$$N_{\text{group}} = 12N_{\text{hydroxyl}} + 12N_{\text{amide}} + 4N_{[-(C=O)-,1]} + 7N_{[-(C=O)-,2]} + 2N_{[-(C=O)-,3]} - N_{(-O-)} + 2N_{[-(NH)-]} - N_{C=C} + 4N_{(\text{special N atom})} \quad (17)$$

where N_{hydroxyl} is the total number of $-OH$ in alcohols or phenols, N_{amide} is the total number of amide groups, $N_{[-(C=O)-,1]}$ is the number of carbonyl groups immediately adjacent to a nitrogen atom without any hydrogen atom attached, $N_{[-(C=O)-,2]}$ is the total number of carbonyl groups in carboxylic acids, ketones and aldehydes, $N_{[-(C=O)-,3]}$ is the total number of carbonyl groups except N_{amide} , $N_{[-(C=O)-,1]}$ and $N_{[-(C=O)-,2]}$, $N_{(-O-)}$ is the number of ether bonds (R-O-R'), $N_{[-(NH)-]}$ is the number of nearby $-(NH)-$ units without carbonyl groups, $N_{C=C}$ is the number of $C = C$ bonds, and $N_{(\text{special N atom})}$ is the number of nitrogen atoms in the six-membered aromatic ring.

$$N_{dc} = 19N_N + 7N_{(BB_{O,S})} + 12N_{(SG_{O,S})} - 14N_{\text{cyc}} + 52N_{\text{sulfone}} - 2N_F + 8N_{ClBrasym} + 20N_{Si} \quad (18)$$

where N_N is the number of nitrogen atoms, $N_{(BB_{O,S})}$ is the total number of oxygen and divalent sulfur atoms on the main chain unrelated to the bonding environment, $N_{(SG_{O,S})}$ is the total number of oxygen and divalent sulfur atoms on the side groups unrelated to the bonding environment. $N_{ClBrasym}$ is the number of chlorine and bromine atoms asymmetrically attached to the same backbone atom.

$$V_W \approx 2.286940^0\chi + 17.140570^1\chi^V + 1.369231N_{vdW} \quad (19)$$

where N_{vdW} is the structural correction parameter of van der Waals volume V_W .

$$N_{vdW} = N_{\text{menonar}} + 0.5N_{\text{mear}} + N_{\text{alamid}} - 4N_{\text{cyc}} + 2N_{\text{cyanide}} + 3N_{\text{carbonate}} + 2N_{C=C} + N_{OH-} - 2.5N_{\text{fused}} + 7N_{Si} - 8N_{(-S-)} - 4N_{Br} \quad (20)$$

where N_{menonar} is the number of methyl groups attached to non-aromatic atoms, N_{mear} is the number of methyl groups directly attached to aromatic ring atoms, N_{alamid} is the total number of bonds between non-aromatic atoms and amide

and urea groups, N_{cyc} is the number of non-aromatic rings without double bonds on the side, N_{cyanide} is the number of $-\text{C}\equiv\text{N}$ groups, $N_{\text{carbonate}}$ is the number of carbonates, $N_{\text{C}=\text{C}}$ is the number of $\text{C}=\text{C}$ bonds in the acyclic structure, N_{OH} is the total number of $-\text{OH}$ groups, N_{fused} is the number of rings in the “thickened” ring structure. N_{Si} is the number of silicon atoms.

It should be noted that to ensure the generality of the calculation method, Eqs. (14)–(20) contain a large number of structural correction terms (Bicerano, 2002). If a specific structure does not exist in the polymer, the corresponding correction parameter is equal to zero. For example, when calculating E_{coh1} for G_1 , $N_{\text{atomic}} = 0$ in Eq. (15).

The results of the dielectric constant calculations for G_1 – G_4 are shown in Table 2. It can be seen from the table that the dielectric constants of the repeating units calculated by the CI method are very close to the measured values of their corresponding homopolymers, indicating that the calculation results of this method are accurate and can well characterize the contribution of nonpolar repeating units to the polymer as a whole.

2.3. Calculation of the dielectric constant of the polar repeating unit

The dielectric constants of the polar repeating units (G_5 , G_6) cannot be calculated by the structure–property analysis method. Molecular dynamics simulations (MDS) based on first principles can predict them (Bicerano, 2002). In this paper, the MDS of polar repeating units are used to calculate their dielectric constants using the DMF method.

A permanent molecular dipole consisting of two charge $\pm q$ at a distance l , giving the dipole moment $\mu = ql$, is shown in Fig. 3. For molecules with complex structures, the dipole moment can be obtained by adding simple dipole moment vectors, as shown in Eq. (21). Similarly, it can be known that the total dipole moment M in a periodic cell is the vector sum of the dipole moments of all molecules in the system.

$$\mu_{i,a} = \sum_{a=1}^N q_{i,a} l_{i,a} \quad (21)$$

where $q_{i,a}$ is the partial charge of the atom a in molecular i and $l_{i,a}$ is the position vector of the atom a in molecular i .

An all-atom model of repeating unit is constructed in the Materials Studio software. On this basis, a periodic cell containing N particles is built for MDS ($N = 256$ (Neumann, 1983)), as shown in Fig. 4. In order to prevent the nesting of molecular structure, we set the initial density to be relatively low, 0.5 g/cm^3 . The reaction force field is COMPASS. The

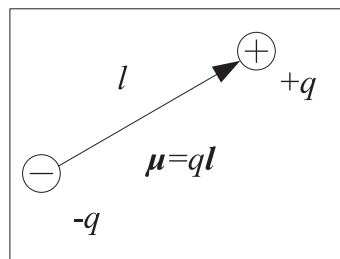


Fig. 3 The schematic representation of a permanent molecular dipole.

temperature control method is Andersen’s algorithm. The pressure control method is Berendsen’s, and the calculation of the non-bonded cooperative force is based on the group-based method. The simulation time step is 1 fs, the cutoff distance is 12.5 \AA , the spline width is 1 \AA , the buffer width is 0.5 \AA , and the pressure is 0.1 MPa.

The periodic cells are geometrically optimized with a convergence standard of 0.001 kcal/mol. The geometrically optimized periodic cells are annealed to make their density close to the real value. The annealing process is carried out in the NPT ensemble with a starting temperature of 300 K, an intermediate maximum temperature of 500 K, and a pressure value of 0.1 MPa. The temperature rise step is set to 50 K, and the number of cycles is 5. 100 000 kinetic steps are performed for each temperature, and one frame of output is performed every 500 steps.

On the basis of a stable conformation, 10 frames with a temperature of 298 K are extracted for NVT dynamics simulation with 400 ps, and the output frame is performed every 100 steps. The dielectric constant values of 10 samples are averaged as the final value to reduce the error. The total dipole moment of the system in each frame was statistically calculated using a Perl script. The total dipole moment M , as a vector, has three components M_x , M_y , and M_z in the x , y , and z directions.

According to molecular theory, the corresponding relationship between dipole moment–time and macroscopic dielectric constant can be constructed (Williams, 1972). For periodic boundary systems, the relationship between total dipole moment–time and macroscopic dielectric constant can be expressed by Eq. (22) (De Leeuw et al., 1980; Heinz et al., 2001).

$$\varepsilon = 1 + \frac{1}{3Vk_B T \varepsilon_0} (\langle M^2 \rangle - \langle M \rangle^2) \quad (22)$$

where V is the volume; k_B is the Boltzmann constant; T is the thermodynamic temperature; ε_0 is the vacuum dielectric con-

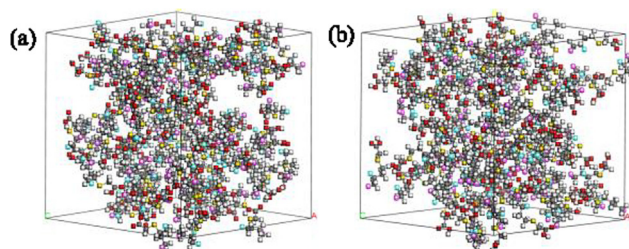


Fig. 4 (a) G_5 's and (b) G_6 's periodic cell model.

Table 2 Dielectric constant calculation results of G_1 – G_4 .

No.	Molar mass	Calculated value	Tested value
G_1	106.168	2.567	2.60(Deby and Bueche, 1951)
G_2	56.108	2.317	–
G_3	56.108	2.317	2.36(Chen, 1971)
G_4	56.108	2.311	–

stant; \mathbf{M} is the total dipole moment of the system; $\langle \rangle$ denotes the Boltzmann system average.

Each output frame of results during the simulation can be interpreted as a sampling of the dynamics simulation system, and Eqs. (23) and (24) can express the Boltzmann averaging term in Eq. (22).

$$\langle M^2 \rangle = \frac{1}{N_s} \sum_{i=1}^{N_s} \mathbf{M}(t_i) \cdot \mathbf{M}(t_i) \quad (23)$$

$$\langle M \rangle^2 = \left[\frac{1}{N_s} \sum_{i=1}^{N_s} \mathbf{M}(t_i) \right]^2 \quad (24)$$

where t_i is the time corresponding to simulation time step i , and N_s is the total number of sampling steps.

To investigate the relationship between the dipole moment fluctuation of the repeating unit and the orientation polarization of the material, we calculated the dielectric constant values for different dipole moment fluctuation times, as shown in Fig. 5. Overall, G_6 has a larger dielectric constant than G_5 , which is caused by the difference in permanent dipole moment μ_0 due to the structural difference. As time increases, the dielectric constant of both G_5 and G_6 first increase and then decrease. This can be explained by the dielectric orientation polarization process. We assume that the different dipole moment fluctuation times correspond to the time of electric field action, as shown by the blue dashed line in Fig. 5. At the electric field value greater than zero, the dipole inside the material undergoes an oriented arrangement, and the polarization intensity is always intensified. The polarization intensity reaches its highest, and the dielectric constant is maximum when the dipole moment fluctuation time is 300 ps. When the electric field direction is flipped, the dipole arrangement inside the material will reverse with the electric field direction. If the statistical time exceeds 300 ps, the statistical result of Eq. (22) decreases, as shown in the figure for 350 ps, 390 ps, and 400 ps. This phenomenon may correspond to the phenomenon of internal polarization of the material under the action of an alternating electric field. Suppose an alternating electric field of voltage amplitude V acts on the material. When the electric field is positive, the polarization intensity inside the material gradually increases. When the electric field is negative, the dipole arrangement inside the material will turn, and the dielectric constant decreases. We intercepted the total dipole

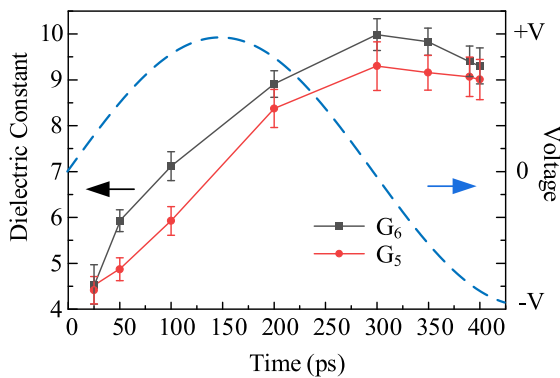


Fig. 5 The dielectric constant of G_5 and G_6 with different simulation times.

moment fluctuation data of G_6 from 300 ps to 400 ps and calculated the dielectric constant as 6.78 using Eq. (22), which is very close to the result of $t = 100$ ps, which is consistent with our proposed conjecture.

2.4. Calculation of dielectric constant of graft-modified SBS

The molar polarizability of the repeating unit can be calculated using three models, Gladstone-Dale, Lorentz-Lorenz, and Vogel, and considering that the molar mass is easier to calculate than the molar volume, the Vogel model is used in this paper. The results calculated according to Eq. (25) are shown in Table 3.

$$P_{Vi} = M_i \sqrt{\epsilon_i} \quad (25)$$

where P_{Vi} , M_i , and ϵ_i are the molar polarizabilities, molar masses, and dielectric constants of the repeating unit G_i .

In a semi-empirical approach, the molar properties of non-interacting substances can be calculated by summing the contributions of atoms, groups, or bonds (Zhou et al., 2014). The molar mass, molar polarizability of polymers can be calculated according to Eqs. (26)–(27).

$$M_p = \sum n_i M_i \quad (26)$$

$$P_{Vp} = \sum n_i P_{Vi} \quad (27)$$

where M_p and P_{Vp} are the molar mass, and molar polarizability of the polymer, respectively, and n_i , M_i , and P_{Vi} are the molar number, molar mass, and molar polarizability of the repeating unit G_i .

Eqs. (26)–(27) are substituted into Eq. (4) yields Eq. (28) for the calculation of the dielectric constant of the polymer. Dividing the upper and lower parts of this equation simultaneously by $\sum n_i$ the Eq. (29) for calculating the dielectric constant of the polymer expressed in terms of molar content is obtained. The molar content was calculated by equation (30) (Tashiro et al., 1984).

$$\epsilon_p = \left(\frac{\sum n_i P_{Vi}}{\sum n_i M_i} \right)^2 \quad (28)$$

$$\epsilon_p = \left(\frac{\sum c_i P_{Vi}}{\sum c_i M_i} \right)^2 \quad (29)$$

$$c_i = \frac{n_i}{\sum n_i} \quad (30)$$

where ϵ_p is the polymer dielectric constant, n_i and c_i are the numbers of moles and molar content of repeating unit G_i per mole of polymer, respectively.

SBS determines the molar content of each repeating unit in SBS-TGA. According to Fig. 1, the molar content of G_1 is equal to that in SBS; G_5 is derived from G_2 and G_3 grafted TGA. The sum of the three is equal to the sum of the molar content of G_2 and G_3 in SBS, and G_6 is derived from G_4 grafted TGA, and the sum of the molar content of the two is equal to the molar content of G_4 in SBS. The C = C located in the side chain is more active and more prone to grafting reactions (Tian et al., 2016; Sun et al., 2016). Therefore, G_4 reacts with TGA first during the grafting process. G_2 and G_3 do not graft TGA until G_4 is completely converted to G_6

Table 3 Molar polarizability of G₁-G₆.

No.	G ₁		G ₂		G ₃		G ₄	
Molar polarizability	170.101		85.092		85.092		85.295	
No.	G ₅ -300ps	G ₅ -200ps	G ₅ -100ps	G ₅ -50ps	G ₅ -25ps			
Molar polarizability	452.036 ± 12.879	428.922 ± 6.874	360.749 ± 9.500	327.051 ± 8.397	314.799 ± 10.468			
No.	G ₆ -300ps	G ₆ -200ps	G ₆ -100ps	G ₆ -50ps	G ₆ -25ps			
Molar polarizability	468.427 ± 8.090	442.461 ± 7.175	395.500 ± 8.749	360.939 ± 7.213	315.682 ± 11.483			

and no G₅ is generated. The relationship between c₁-c₆ in SBS-TGA can be written and expressed as Eq. (31).

$$\begin{cases} c_1 = c_{1,SBS} \\ c_2 + c_3 + c_5 = c_{2,SBS} + c_{3,SBS} \\ c_4 + c_6 = c_{4,SBS} \\ 0 \leq c_5 \leq c_{2,SBS} + c_{3,SBS} \\ 0 \leq c_6 \leq c_{4,SBS} \\ \text{if } c_6 < c_{4,SBS}, \text{ then } c_5 = 0 \end{cases} \quad (31)$$

where c_i(i = 1, 2, ..., 6) means the molar content of repeating unit G_i in SBS-TGA, and c_{i,SBS}(i = 1, 2, 3, 4) means the molar content of repeating unit G_i in SBS.

According to SBS's H Nuclear Magnetic Resonance (HNMR) (Ellingford et al., 2018) and specific area analysis method $c_{1,SBS} = 18\%$, $c_{2,SBS} + c_{3,SBS} = 60\%$, $c_{4,SBS} = 22\%$.

The variation of G₅ and G₆ molar content in SBS-TGA corresponds to the variation of TGA grafting rate in polybutadiene blocks. Therefore, the equation for the grafting rate of SBS-TGA is shown in Eq. (32), and the variation law of dielectric constant with grafting rate is shown in Fig. 6.

$$g_r = \frac{c_5 + c_6}{c_2 + c_3 + c_4 + c_5 + c_6} \times 100\% \quad (32)$$

It can be seen from the figure that the constant dielectric increases gradually with the increase of the grafting rate. The dielectric constant of unmodified SBS is 2.4 when the grafting rate is 0. Under the same polarization time, the higher the grafting rate, the greater the dielectric constant, and the maximum value can reach 8.3, which is 3.5 times the initial value. Therefore, for SBS-TGA, increasing its dielectric constant can be achieved by changing the reaction conditions to increase the grafting rate of TGA.

3. Experimental validation

3.1. Materials

SBS (YH-806) is produced by Baling Petrochemical, China, Tetrahydrofuran (THF, AR grade) and Cyclohexane (AR grade) are purchased from Kelon Chemical Co., Ltd., China, 2,2-dimethoxy-2-phenyl acetophenone (DMPA, 99%) and TGA (AR grade, 96%) were purchased from Shanghai Aladdin Biochemical Technology Co., Ltd., China. All of the above chemicals were not processed before use.

3.2. Synthesis

The reaction principle was mercapto-olefin reaction under UV irradiation, and the catalyst was DMPA. The molar ratio of the sulfhydryl group to the C = C bond was set to 5:1 during the synthesis.

In the first step, SBS and tetrahydrofuran were placed in a beaker at the ratio of 1:9 by weight and stirred magnetically at 30 °C until SBS was dissolved entirely, and 50 g of the dissolution solution was used for material preparation. In the second step, 0.1 g of DMPA and 29.9 g of TGA were added to the SBS dissolution solution. Finally, the SBS-TGA was extracted from the solution with cyclohexane, filtered, and dried under vacuum at 60 °C for 24 h. The grafting rate of the SBS-TGA was determined by the use of a UV lamp with a wavelength of 365 nm and a power of 50 W. In the third step, the SBS-TGA was extracted from the solution with cyclohexane, filtered, and dried under vacuum for 24 h at 60 °C.

3.3. Film sample preparation

The samples were prepared using a manual hot press machine model AR1701 from AUPLEX Co., Ltd., China. The raw material was placed in the mold at 150 °C and kept under nor-

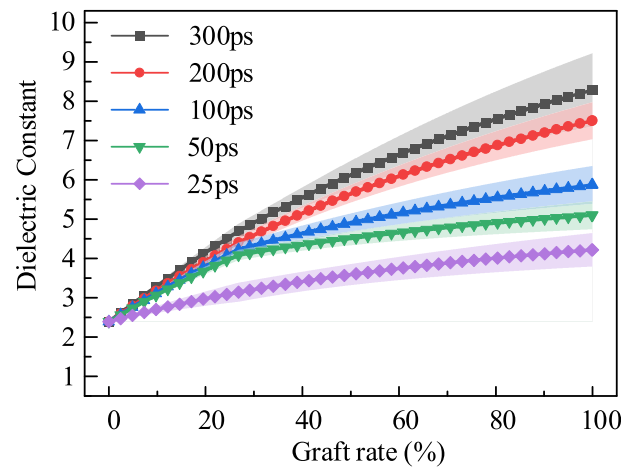


Fig. 6 Calculated value of the dielectric constant of SBS-MT with different grafting rate.

mal pressure for 15 min to eliminate air bubbles, and the pressure was adjusted to 2.5 MPa and kept for 10 min. The mold was removed, cooled to room temperature, and then the film samples were taken out with a thickness of about 0.5 mm.

3.4. Calculation of grafting rate

The HNMR spectrum was measured using a Bruker AV600MHz high-resolution liquid NMR spectrometer with a solvent of CDCl₃ and a chemical shift range of 0–8 ppm. The test results are shown in Fig. 7.

It can be seen from the figure that the characteristic peaks corresponding to C = C gradually decreased, and the characteristic peaks associated with TGA gradually increased with the increase of reaction time, which indicated that the grafting rate of SBS-TGA gradually increased. The area integrals of the characteristic peaks of the G₁-G₆ repeat units were calculated on the HNMR spectra with the benzene ring H as the reference, and the grafting rate of SBS-TGA could be calculated using the specific area method as shown in Eq. (33). The calculated results showed that the grafting rates of the three SBS-TGA samples were 15.3%, 47.2%, and 89.7%, respectively. The grafting rate gradually increased with the increase of reaction time.

$$g_r = \left(1 - \frac{S_{C=C}/S_{St}}{S_{C=C}/S_{St}}\right) \times 100\% \quad (33)$$

where g_r is the grafting rate, S_{St} is the integral area corresponding to the benzene ring on the HNMR spectrum, $S_{C=C}$ is the integral area corresponding to C = C before grafting, and $S_{C=C}$ is the integral area corresponding to C = C after grafting.

3.5. Dielectric constant test

Measurements were performed using a Concept 80 broadband dielectric test system with an electrode diameter of 20 mm. The polarization ability of the material was enhanced after grafting dipole, and the dipole polarization time range was 10^{-10} - 10^{-2} s, corresponding to a frequency range of 10^2 - 10^{10} Hz, and considering the measurement range of the equipment, the test frequency range of 10^2 - 10^6 Hz was chosen in this paper. The variation curve of the real part of the dielectric constant with frequency is shown in Fig. 8.

The dielectric constant of SBS is basically not affected by frequency. This is because SBS is nonpolar, and the polarization phenomenon under the action of an electric field is mainly induced polarization, and the molecular polarization rate does not change within the measurement frequency range. The dielectric constant of SBS-TGA will gradually increase as the measurement frequency decreases. According to Eq. (5) and related analysis, the lower the frequency, the longer the electric field action time, the more orderly arrangement of the dipoles, and the greater the polarization intensity, which corresponds to a greater dielectric constant. The dielectric constant of SBS-TGA gradually increases with the increase of grafting rate. This is because the permanent dipole μ_0 inside the material increases after grafting TGA. According to Eq. (5), the higher the grafting rate, the greater the polarization intensity at the same test frequency and the greater the dielectric constant. The difference in the dielectric constant of SBS-TGA

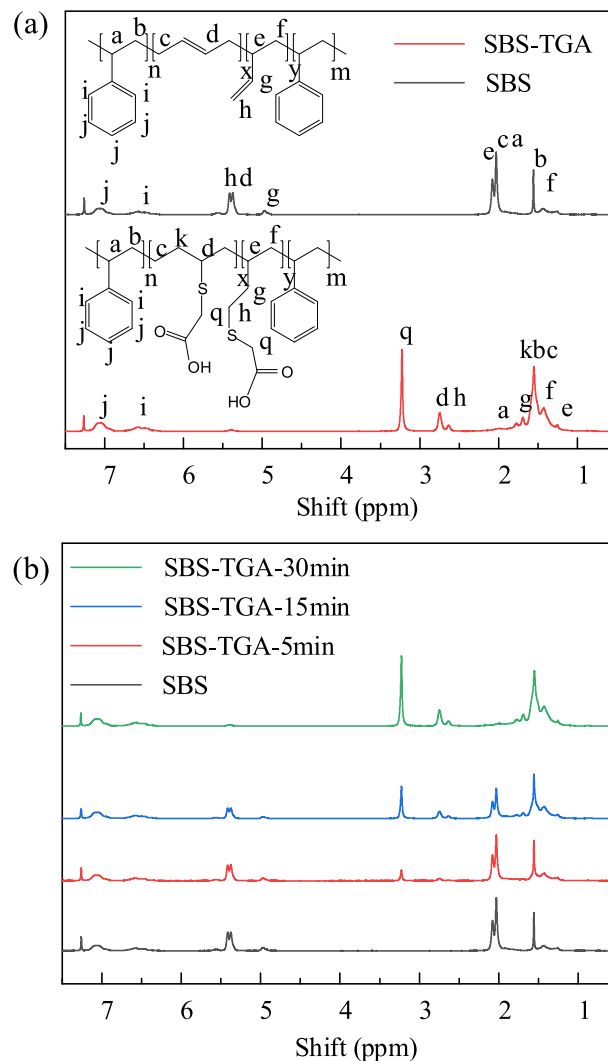


Fig. 7 HNMR of SBS and SBS-TGA, (a) Chemical shifts of hydrogen atoms on the main functional groups, (b) HNMR of SBS-TGA with different grafting rates.

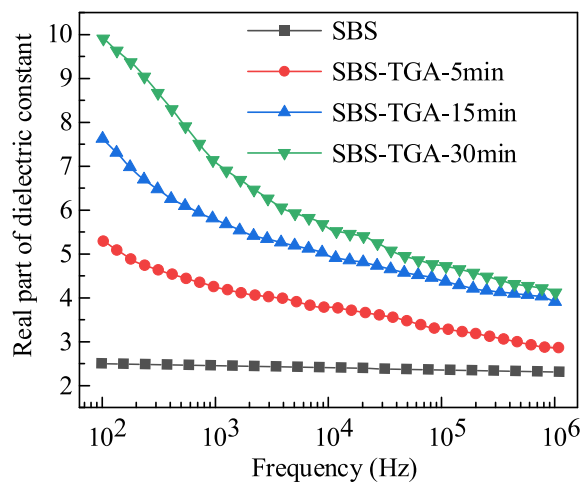


Fig. 8 The real part of the dielectric constant of SBS and SBS-TGA.

with different grafting rates decreases as the frequency increases. This is because higher frequency means shorter dipole turning time and lower molecular polarizability. This leads to a decrease in the difference in the dielectric constant of SBS-TGA materials with different grafting rates.

3.6. Analysis of results

We choose five sets of data for comparison, as shown in Fig. 9. The experimental test values are selected at 0.1 kHz, 1 kHz, 10 kHz, 100 kHz, 1000 kHz, and the dipole moment fluctuation times are selected at 300 ps, 200 ps, 100 ps, 50 ps, and 25 ps, respectively. The difference between the test value at 0.1 kHz and the calculated value of 300 ps is very large for the first set of data, and the reason for this phenomenon is put in the following paragraphs. We can summarize the relationship between the test frequency and the dipole moment fluctuation time by using Eq. (34).

$$t = 200 \times 2^{-1 \lg f} \quad (34)$$

where t is the dipole moment fluctuation time in the DMF calculation process, in ps, and f is the frequency in the broadband dielectric spectrum test process, in kHz.

We take the DMF time $t_1 = 45$ ps, $t_2 = 150$ ps, and $t_3 = 300$ ps into Eq. (34) respectively, and calculate the corresponding frequency values $f_1 = 141.9$ kHz, $f_2 = 2.6$ kHz, $f_3 = 0.26$ kHz. The calculated and measured dielectric constant of different samples is shown in Table 4.

Examples 1 and 2 demonstrate that the theoretical calculations match the measured values relatively well in the higher frequency range, 1 kHz-1000 kHz. Example 3 shows that when the frequency is below 1 kHz, there is a significant deviation

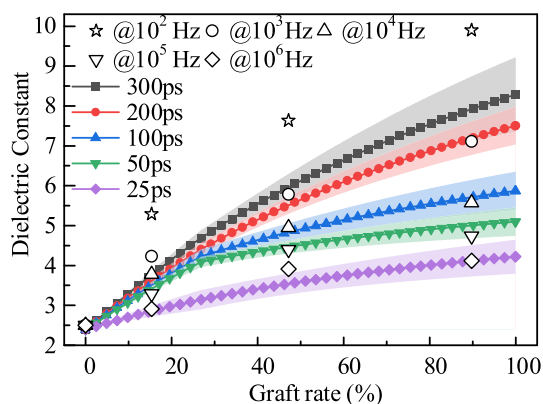


Fig. 9 Comparison of experimental value and calculated value for dielectric constant.

between the theoretical calculation and the measured value. At below 1 kHz, space charge polarization may occur within the material in addition to dipole shifting polarization, which further increases the overall material polarization intensity and results in larger measured dielectric constant values. The DMF method cannot take into account the space charge polarization process, so the proposed dielectric constant calculation method in this paper cannot perform dielectric constant prediction below 1 kHz. The applicability of the method in the higher frequency range has not been verified due to the measurement error of the experimental equipment and the accuracy of the software calculation. Therefore, the proposed method for calculating the dielectric constant of block copolymers is applicable in the frequency range of 1 kHz to 1000 kHz.

4. Conclusion

In this paper, a method for calculating the permittivity of non-polar/polar block copolymers was proposed using SBS-TGA as the research object, and theoretical calculations and experimental tests proved the validity of the method. The main conclusions are as follows.

- 1) Based on the group contribution theory, the modified SBS molecular chains were split, and the group contribution values of nonpolar repeating units and polar repeating units were calculated using the CI method, the DMF method and Vogel model, and a hybrid calculation method of dielectric constants of block copolymers without relying on experimental data was proposed.
- 2) The grafting rate of polar groups can adjust the dielectric constant value of modified SBS. Theoretical calculations and experimental tests show that the higher the grafting rate, the higher the dielectric constant of modified SBS. We also summarized the conversion relationship from theoretical calculation to experimental test. The applicable frequency range of the proposed method is 1 kHz to 1000 kHz.
- 3) In the development of new polymer dielectric materials, this method can guide the screening of grafting groups and determine reactant ratios, which is essential for improving the efficiency of research and development.

5. Data available statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Table 4 Comparative examples of calculation and test.

SBS-TGA	Example 1		Example 2		Example 3	
	t_1	f_1	t_2	f_2	t_3	f_3
5 min	3.14	3.23	3.48	3.61	7.98	8.92
15 min	4.04	4.28	4.94	4.72	5.96	6.63
30 min	4.63	4.64	6.03	5.25	3.74	4.71

CRediT authorship contribution statement

Youyuan Wang: Conceptualization, Methodology, Investigation, Writing – original draft, Visualization. **Zhanxi Zhang:** Resources, Methodology, Writing – review & editing. **Rongliang Zheng:** Software, Formal analysis. **Yanfeng Zhang:** Supervision, Conceptualization, Methodology, Writing – review & editing.

Declaration of Competing Interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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