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ORIGINAL ARTICLE

Theoretical study of the structure and fundamental properties of $A\text{Zn}_2\text{N}_2$ ($A = \text{Ca}, \text{Sr}, \text{Ba}$)



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Abstract The structure, stability, elastic, electronic, and optical properties of trigonal AZn_2N_2 ($A = \text{Ca}, \text{Sr}, \text{Ba}$) are simulated and compared in this work. The stability and physical properties of BaZn_2N_2 are mainly highlighted. According to the calculated results, three compounds are thermodynamically and mechanically stable, and they are brittle materials. The stability of trigonal BaZn_2N_2 is confirmed by using the different theoretical approaches. The direct band gap transition is allowed at the Γ point for each compound. The predicted direct band gaps are 1.733, 1.507, and 1.510 eV for CaZn_2N_2 , SrZn_2N_2 , and BaZn_2N_2 , respectively. The valence band is mostly composed of the N-2p orbitals, while the conduction band is mainly contributed from the Ca-3d/Sr-4d/Ba-5d orbitals. The results show that the electron shows high mobility for carrier transport, and the value of exciton binding energy is less than 80 meV. Furthermore, compared to CaZn_2N_2 and SrZn_2N_2 , BaZn_2N_2 shows excellent light absorption capacity in the visible region. This study indicates that BaZn_2N_2 is a desirable material for solar cell applications.

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1. Introduction

The most representative nitrides are GaN and its alloys such as $\text{Ga}_{1-x}\text{Al}_x\text{N}$ and $\text{Ga}_{1-x}\text{In}_x\text{N}$ because they are the important materials for optoelectronic devices (Ul Haq et al., 2014; Özdemir et al., 2019).

The electronic, optical, and thermoelectric properties of two-dimensional III-nitrides $\text{Ga}_{1-x}\text{Al}_x\text{N}$ and $\text{Ga}_{1-x}\text{In}_x\text{N}$ have been demonstrated through density functional theory (DFT) calculations (Wines et al., 2020). However, these compounds contain the rare or toxic elements, which is difficult to achieve large-scale commercial applications. Therefore, it is of great importance to explore novel nitrides, which are composed of earth-abundant and non-toxic elements. The fundamental physical properties of II–IV–N₂ nitrides and their alloys have been investigated in recent years, such as ZnSiN₂ (Häusler et al., 2017; Mallmann et al., 2019); ZnGeN₂ (Häusler et al., 2017; Mallmann et al., 2019); MgSiN₂ (Mallmann et al., 2019; Häusler et al., 2018); MgGeN₂ (Mallmann et al., 2019; Häusler et al., 2018); ZnSnN₂ (Cao et al., 2017; Laidouci et al., 2020; Tsunoda et al., 2018), and Zn_{1-x}Mg_xSnN₂ (Yamada et al., 2021).

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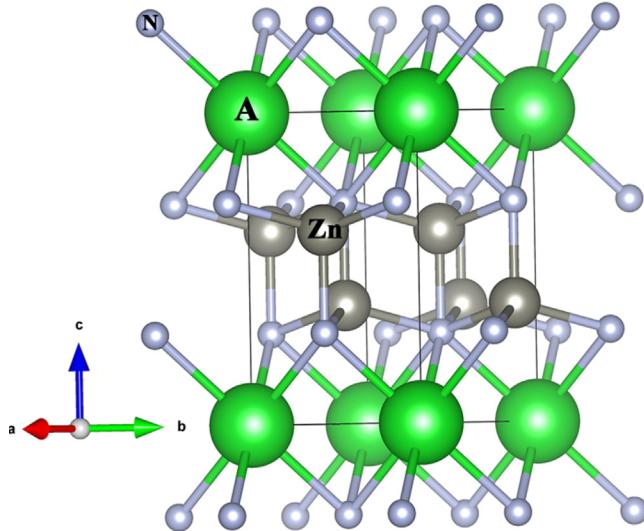


Fig. 1 The trigonal structure of AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$).

The computational screening of ternary nitrides is conducted, and some novel compounds are finally identified (Hinuma et al., 2016). For example, CaZn_2N_2 can be synthesized by high-pressure methods, and it is a direct band gap semiconductor with 1.8 eV (Hinuma et al., 2016). The band gap energy of CaZn_2N_2 is narrowed to 1.6 eV by the substitution of Sr for Ca, which is further confirmed by the recent experiment (Kikuchi et al., 2021). In addition, the direct band gap can be widely tuned from ~ 1.8 to ~ 3.2 eV between CaZn_2N_2 and CaMg_2N_2 (Tsuiji et al., 2019). CaZn_2N_2 is a promising candidate for next-generation semiconductor in the field of light-emitting diodes and solar cells (Tsuiji et al., 2019; Huang et al., 2022). A detailed theoretical study is performed to reveal the impact of pressure on the dynamical, elastic, and thermal properties of CaZn_2N_2 (Zhao et al., 2017). The structure and fundamental physical properties of MgBe_2N_2 , CaBe_2N_2 , CaMg_2N_2 , SrMg_2N_2 , CaZn_2N_2 , and SrZn_2N_2 are thoroughly studied via first-principles calculations (Khan et al., 2019; Khan et al., 2018; Khan et al., 2018; Murtaza et al., 2018; Murtaza et al., 2018; Murtaza et al., 2018). It is revealed from our recent theoretical work that the band gaps of CaZn_2N_2 and SrZn_2N_2 are effectively regulated by the partial substitution of Cd for Zn (Liu et al., 2022).

The structures and physical properties of both CaZn_2N_2 and SrZn_2N_2 have been reported experimentally and theoretically (Hinuma et al., 2016; Kikuchi et al., 2021; Zhao et al., 2017). However, no available experimental and theoretical reports are conducted for exploring the fundamental properties of BaZn_2N_2 . Therefore, a comprehensive study is required to investigate the structure, stability, elastic, electronic, and optical properties of BaZn_2N_2 . Moreover, it is vital to know whether the trigonal phase is stable for BaZn_2N_2 . The thermodynamic, dynamic, thermal, and mechanical stability of BaZn_2N_2 is

Table 2 The atomic coordinates for BaZn_2N_2 .

Atom	<i>x</i>	<i>y</i>	<i>z</i>
Ba	0.00000	0.00000	0.00000
Zn1	0.33333	0.66667	0.62018
Zn2	0.66667	0.33333	0.37982
N1	0.33333	0.66667	0.29112
N2	0.66667	0.33333	0.70888

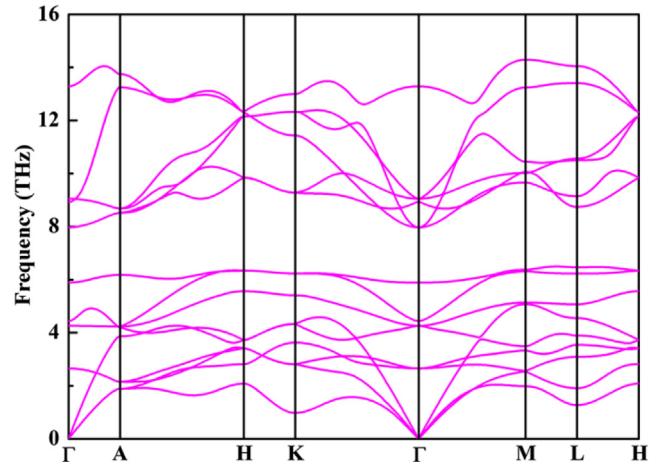


Fig. 2 The phonon spectrum curves of trigonal BaZn_2N_2 .

evaluated for the first time. The elastic, electronic, and optical properties of AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$) are compared and discussed in detail. The influence of different cations on the various physical properties of AZn_2N_2 is revealed. The results suggest that BaZn_2N_2 is a stable and desirable material for solar cell applications.

2. Computational details

The structure and physical properties of trigonal AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$) were simulated in this work by using first-principles calculations as implemented in the Vienna ab initio simulation package (VASP) (Kresse and Furthmüller, 1996). The interaction between ions and valence electrons was dealt by the projector augmented wave (PAW) (Blöchl, 1994) method. The structure was fully relaxed by employing Perdew–Burke–Ernzerhof (PBE) functional within the generalized gradient approximation (GGA) (Perdew et al., 1996). The

Table 1 The various structural parameters for AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$).

Compound	$a = b$ (Å)	c (Å)	V (Å 3)	$\alpha = \beta$ (°)	γ (°)	$\text{A} - \text{N}$ (Å)
CaZn_2N_2	3.48	6.04	63.35	90	120	2.54
Exp. ^a	3.46	6.01	/	/	/	/
Theor. ^a	3.45	5.99	/	/	/	/
SrZn_2N_2	3.57	6.28	69.47	90	120	2.69
Theor. ^b	3.48	6.15	/	/	/	/
BaZn_2N_2	3.66	6.60	76.64	90	120	2.86

^a Hinuma et al. (2016).

^b Kikuchi et al. (2021).

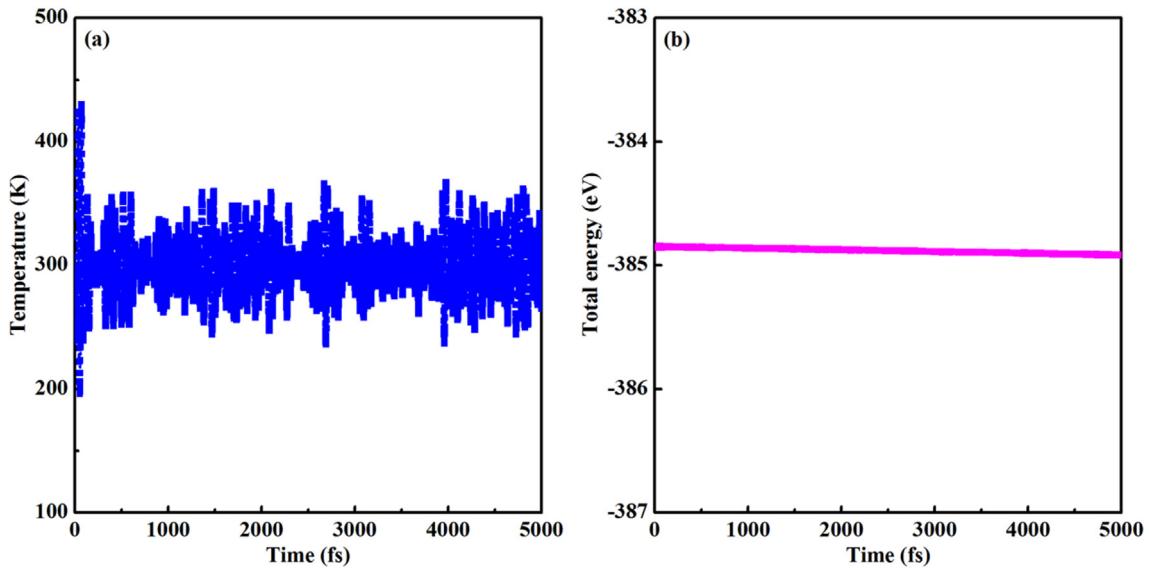


Fig. 3 The variations of (a) temperature and (b) total energy for BaZn_2N_2 at the AIMD simulations.

cut-off energy was set to be 520 eV. The k -point mesh of $8 \times 8 \times 4$ was adopted for all calculations. The convergence criteria of total energy and the forces on each atom were less than 10^{-6} eV and 10^{-3} eV/Å, respectively. The electronic and optical properties of AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$) were obtained by employing the hybrid functional HSE06 (Heyd et al., 2003). A $3 \times 3 \times 2$ supercell was constructed for trigonal BaZn_2N_2 in order to calculate the phonon dispersion curves based on the Phonon code (Togo and Tanaka, 2015). Furthermore, ab initio molecular dynamics (AIMD) simulations were performed for trigonal BaZn_2N_2 at room temperature (300 K).

3. Results and discussion

3.1. Structural properties and stability

The compound AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}$) crystallizes in the trigonal structure (space group: $P\bar{3}m1$) (Hinuma et al., 2016; Kikuchi et al., 2021), while the trigonal crystal structure is not reported experimentally for BaZn_2N_2 so far. Therefore, the trigonal crystal structure of BaZn_2N_2 was constructed by substituting Ba for Ca in CaZn_2N_2 . In addition, the physical properties of both CaZn_2N_2 and SrZn_2N_2 are presented in order to explore the effect of different cations on the structure and properties of AZn_2N_2 . Fig. 1 depicts the trigonal crystal structure of AZn_2N_2 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$). The obtained structural parameters of three compounds are demonstrated in Table 1. The lattice constants of CaZn_2N_2 and SrZn_2N_2 are consistent with the recent experimental and theoretical data (Hinuma et al., 2016; Kikuchi et al., 2021). The lattice constant and bond length are increased from CaZn_2N_2 to BaZn_2N_2 . The computed lattice constants of BaZn_2N_2 are $a = b = 3.6$ Å and $c = 6.60$ Å, respectively. The atomic coordinates in the trigonal structure of BaZn_2N_2 are listed in Table 2.

The thermodynamic stability of three compounds is checked by the following formation energy (E_f) formula:

$$E_f = E_{\text{AZn}_2\text{N}_2} - E_{\text{A}} - 2 \times E_{\text{Zn}} - E_{\text{N}_2} \quad (1)$$

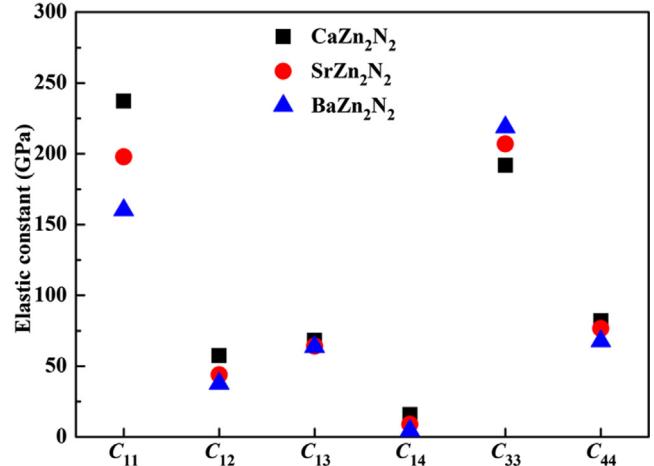


Fig. 4 The trend of six independent elastic constants for CaZn_2N_2 , SrZn_2N_2 , and BaZn_2N_2 .

The calculated values of E_f are -1.94 , -1.37 , and -0.64 eV/f.u., respectively. The results indicate that three compounds can be synthesized at proper conditions and also confirm their thermodynamic stability. It is well known that the lower the E_f , the better the stability, thus the thermodynamic stability is reduced from CaZn_2N_2 to BaZn_2N_2 . Furthermore, it is vital to assess the dynamical stability of trigonal BaZn_2N_2 . The computed phonon dispersion curves are illustrated in Fig. 2. It is dynamically stable for trigonal BaZn_2N_2 because there is no negative frequency. It is observed that three acoustic phonon frequencies are zero at the Γ point, which ensure the dynamical stability of BaZn_2N_2 . It is noted for BaZn_2N_2 that although the tetragonal structure has a lower total energy (~ 80 meV/f.u.) than that of the trigonal structure, the tetragonal structure is not dynamically stable because there are many negative frequencies according to the calculations of phonon spectrum. The AIMD simulations are conducted to further verify the thermal stability of BaZn_2N_2 . As shown in

Fig. 3, it is widely fluctuated for the temperature, but the total energy varies little throughout the whole simulation. The trigonal structure is still maintained, thus the thermal stability is proved.

3.2. Mechanical properties

The elastic properties of CaZn_2N_2 , SrZn_2N_2 , and BaZn_2N_2 are calculated for the first time. It is widely known that there are six independent elastic constants for a trigonal crystal system. The complete Born stability criteria for a trigonal system is the following four conditions (Mouhat and Coudert, 2014):

$$\begin{aligned} C_{11} > |C_{12}|, C_{13}^2 < \frac{1}{2}C_{33}(C_{11} + C_{12}), C_{44} > 0, C_{14}^2 \\ &< \frac{1}{2}C_{44}(C_{11} - C_{12}) \end{aligned} \quad (2)$$

The six elastic constants are displayed in **Fig. 4**. It is verified that three compounds are mechanically stable since all the mentioned conditions are met. It is apparent that five elastic constants (such as C_{11} , C_{12} , C_{13} , C_{14} , and C_{44}) are decreased from CaZn_2N_2 to BaZn_2N_2 , while the only elastic constant C_{33} is increased. The bulk modulus (B) and the shear modulus (G) can be computed by applying the Voigt–Reuss–Hill approximations (Hill, 1952). The Poisson's ratio (ν) is obtained by the formula: $\nu = (3B - G)/[2(3B + G)]$

(Wu et al., 2007). Two parameters of B/G and ν can discern the brittleness or ductility feature of a compound. If the values of B/G and ν are less than 1.75 and 0.26, the compound is brittle, otherwise, the ductile behavior is observed (Hadie et al., 2017; Pugh, 1954). The results show that the values of B/G and ν are in the range of 1.41–1.49 and 0.21–0.23, respectively. It can be inferred that three compounds are brittle materials in nature.

3.3. Electronic properties

The band structure and transition dipole moment (TDM) in the Brillouin zone of each compound are calculated at the PBE functional. First of all, it can be seen from **Fig. 5** that they are direct band gap semiconductors with the valence band maximum (VBM) and conduction band minimum (CBM) at the Γ point. Secondly, the degree of direct electronic transition between the VBM and CBM edges is mainly determined by the value of TDM. According to the previous detailed theoretical study (Meng et al., 2017), there are four types of transitions: (i) all k points forbidden, (ii) partial k points forbidden, (iii) weak transition allowed, and (iv) strong transition allowed. The values of TDM at various k points are illustrated in **Fig. 5**. It is clear that the allowed and strong transition between the band edges at the Γ point is revealed for the studied three compounds, which is desirable for solar cell applications.

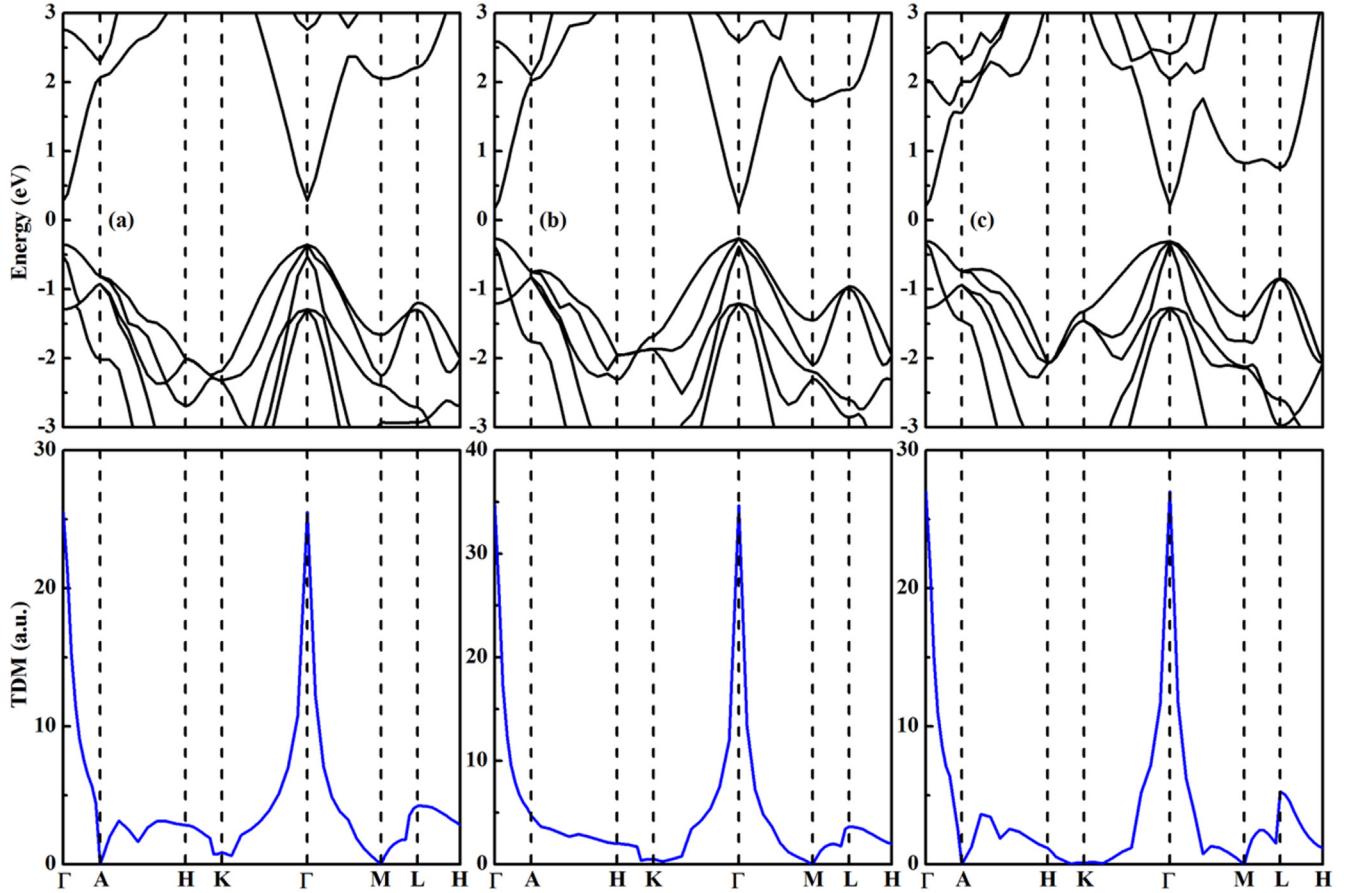


Fig. 5 The band structures (upper) and transition dipole moments (lower) of (a) CaZn_2N_2 , (b) SrZn_2N_2 , and (c) BaZn_2N_2 at the PBE functional.

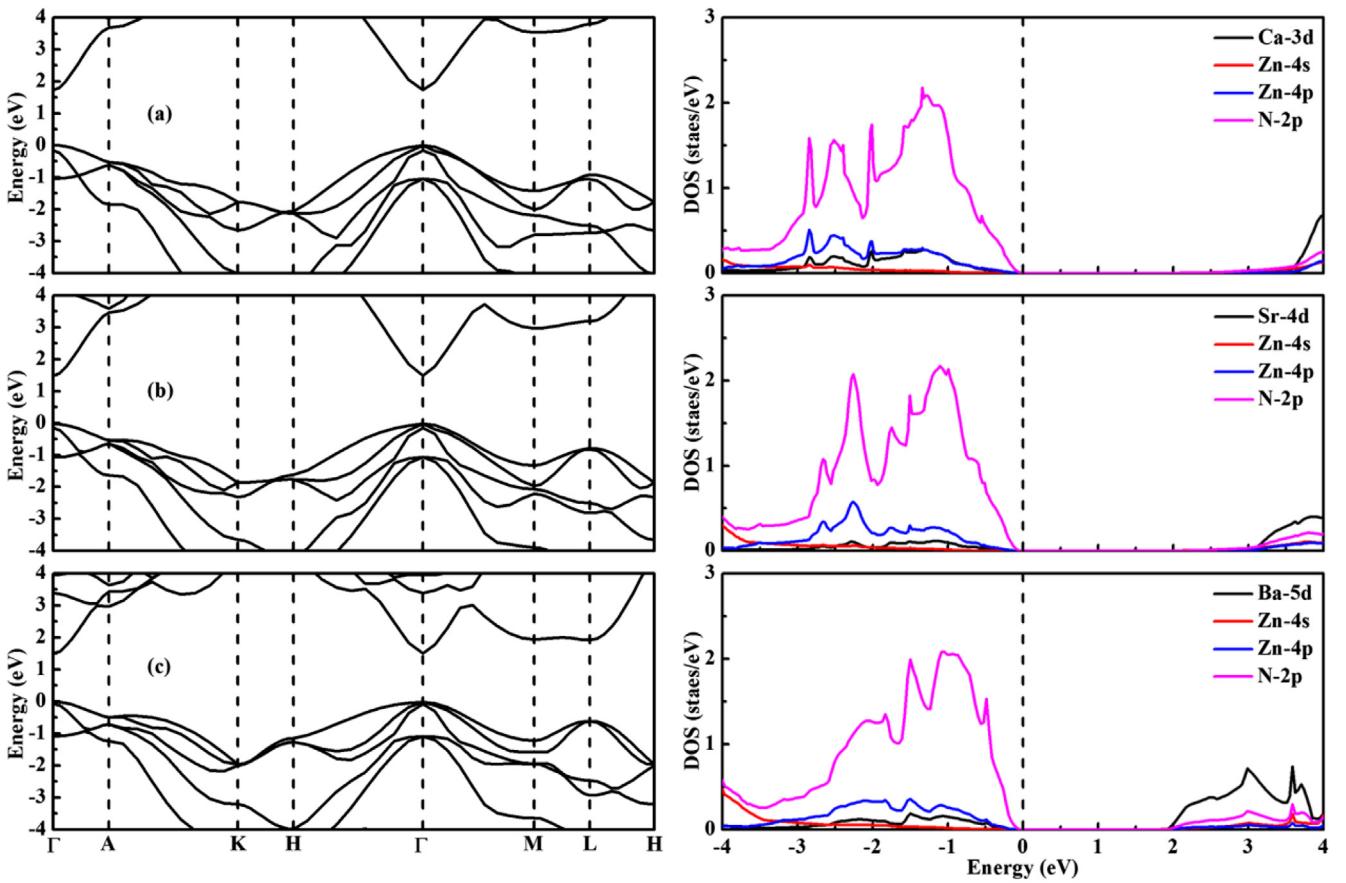


Fig. 6 Band structures (left) and density of states (right) of (a) CaZn₂N₂, (b) SrZn₂N₂, and (c) BaZn₂N₂.

Table 3 The computed values of m_e^* , m_h^* , m_r^* , ϵ , and E_b for AZn₂N₂ (A = Ca, Sr, Ba).

Compound	m_e^* (m_0)	m_h^* (m_0)	m_r^*	ϵ	E_b (meV)
CaZn ₂ N ₂	0.209	1.374	0.181	5.705	76
SrZn ₂ N ₂	0.217	1.345	0.187	5.942	72
BaZn ₂ N ₂	0.244	1.317	0.206	6.637	63

The calculated band gaps are 0.637 and 0.442 eV for CaZn₂N₂ and SrZn₂N₂ when the standard PBE functional is used. The theoretical band gaps of both compounds are seriously underestimated compared to the experimental values (Kikuchi et al., 2021; Tsuji et al., 2019). The corrected band gaps calculated from the HSE06 functional are 1.733 and 1.507 eV for CaZn₂N₂ and SrZn₂N₂, which are reasonable consistent with the recent experimental data (1.8 eV for CaZn₂N₂ and 1.6 eV for SrZn₂N₂) (Kikuchi et al., 2021; Tsuji et al., 2019). It is concluded that the lower band gap can be realized for AZn₂N₂ by varying the earth-alkali metal element. It is observed from Fig. 6 that BaZn₂N₂ is also a direct band gap compound at the Γ point. It is interesting that the direct band gap is 1.510 eV for BaZn₂N₂. It is noted that the band gap difference between SrZn₂N₂ and BaZn₂N₂ is negligible. By analyzing the density of states of three compounds, it is disclosed that the VBM is largely contributed from the N-2p orbitals, while the CBM is dominated by the contribution from the Ca-3d/Sr-4d/Ba-5d orbitals. The contributions from the Zn-4 s and Zn-4p orbitals are little for the edges of VBM and CBM.

The mobility of the carriers is a crucial index for optoelectronic applications. The effective masses of electron (m_e^*) and hole (m_h^*) can be derived from the curvatures around the VBM and CBM with the following relation (Green, 1990):

$$m^* = \hbar^2 \left[\frac{\partial^2 \epsilon(k)}{\partial k^2} \right]^{-1} \quad (3)$$

where \hbar and $\epsilon(k)$ are the reduced Planck constant and orbit eigenvalue, respectively. In addition, the exciton binding energy (E_b) can be further obtained by the following equation (Liu et al., 2021):

$$E_b \approx \frac{13.56 m_r^*}{m_0 \epsilon^2} \quad (4)$$

where m_r^* , m_0 , and ϵ are the reduced effective mass ($m_r^* = m_e^* \times m_h^*/(m_e^* + m_h^*)$), static electron mass, and static dielectric constant, respectively. The effective masses of electron (m_e^*) and hole (m_h^*) along with the $\Gamma \rightarrow A$ direction are computed for AZn₂N₂ (A = Ca, Sr, Ba). It can be seen from Table 3 that

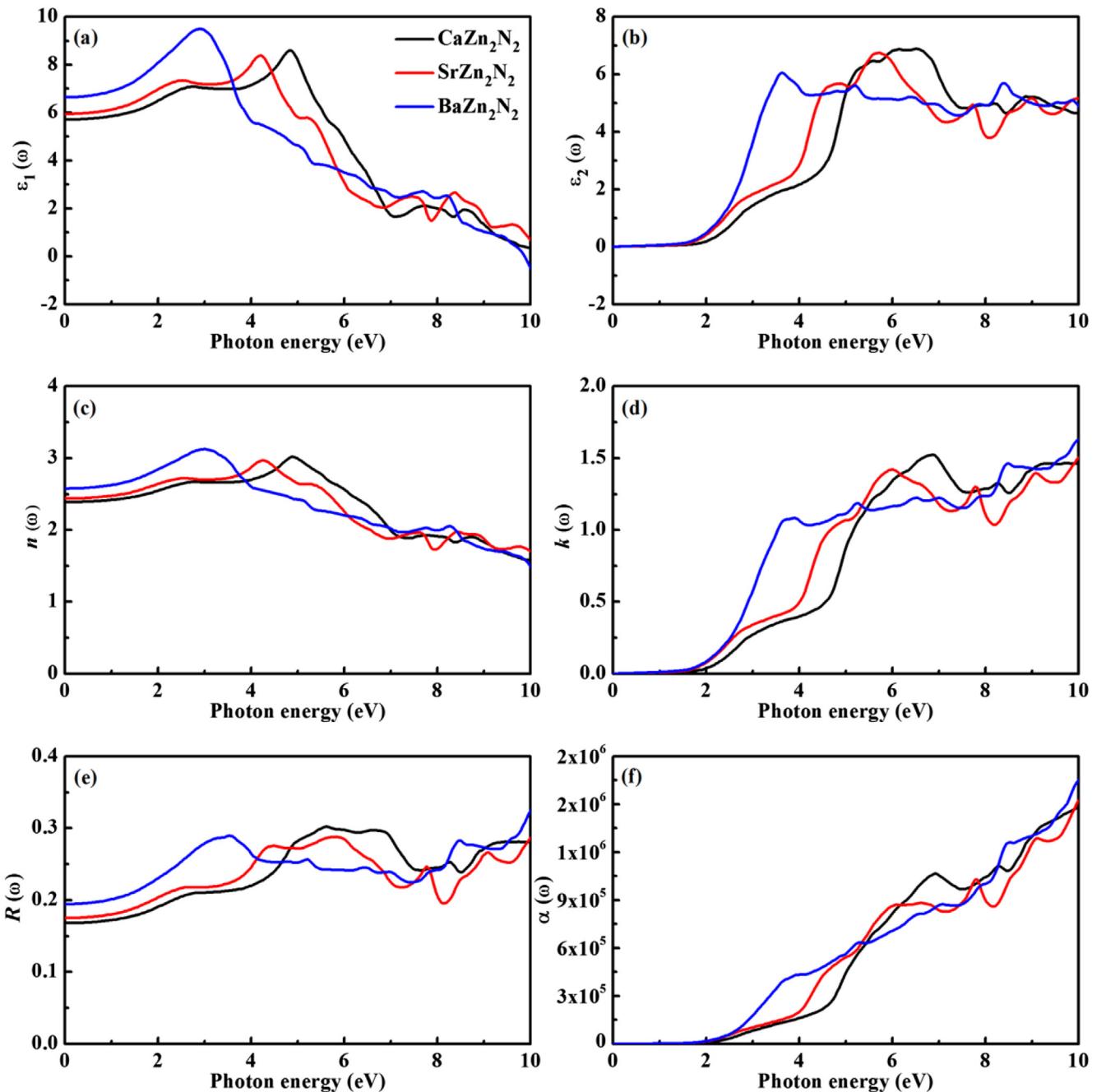


Fig. 7 The optical properties of $A\text{Zn}_2\text{N}_2$ ($A = \text{Ca}, \text{Sr}, \text{Ba}$): (a) $\varepsilon_1(\omega)$, (b) $\varepsilon_2(\omega)$, (c) $n(\omega)$, (d) $k(\omega)$, (e) $R(\omega)$, and (f) $\alpha(\omega)$.

the effective masses of electron and hole are in the range of 0.2–0.3 m_0 and 1.3–1.4 m_0 , respectively. There is an inverse relationship between the effective mass and conductivity (Khan et al., 2021), so the electron shows better mobility for carrier transport. The value of E_b varies between 60 and 80 meV, which indicates that each compound is suitable for application as an absorption layer in solar cells.

3.4. Optical properties

The light harvesting capacity of a semiconductor material is a crucial index for photovoltaic applications. The various optical properties are directly related to the dielec-

tric function $\varepsilon(\omega)$, which is given as follows (Tang et al., 2019):

$$\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2(\omega) \quad (5)$$

where $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ represent the real part and imaginary part of the dielectric function, respectively. The calculated curves of $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ are shown in Fig. 7(a-b). The values of static dielectric constants $\varepsilon_1(0)$ are 5.70, 5.94, and 6.64 for CaZn_2N_2 , SrZn_2N_2 , and BaZn_2N_2 , respectively. The $\varepsilon_2(\omega)$ peak of BaZn_2N_2 is higher than those of CaZn_2N_2 and SrZn_2N_2 in the photon energy range from 2 to 5 eV, indicating that BaZn_2N_2 has better absorption capacity for visible light.

In addition, the refractive index $n(\omega)$, extinction coefficient $k(\omega)$, reflectivity $R(\omega)$, and absorption coefficient $\alpha(\omega)$ of CaZn₂N₂, SrZn₂N₂, and BaZn₂N₂ are computed by the following relations (Zhao et al., 2021):

$$n(\omega) = \left[\frac{\varepsilon_1(\omega)}{2} + \frac{\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)}}{2} \right]^{\frac{1}{2}} \quad (6)$$

$$k(\omega) = \left[\frac{-\varepsilon_1(\omega)}{2} + \frac{\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)}}{2} \right]^{\frac{1}{2}} \quad (7)$$

$$R(\omega) = \frac{[n(\omega) - 1]^2 + k^2(\omega)}{[n(\omega) + 1]^2 + k^2(\omega)} \quad (8)$$

$$\alpha(\omega) = \sqrt{2}\omega \left[\sqrt{\varepsilon_1(\omega)^2 + \varepsilon_2(\omega)^2} - \varepsilon_1(\omega) \right]^{1/2} \quad (9)$$

The calculated results are plotted in Fig. 7(c-f). It can be seen that the curves of $n(\omega)$ and $k(\omega)$ are similar to those of $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$. The static value of refractive index $n(0)$ can be obtained by the equation $n(0) = \sqrt{\varepsilon_1(0)}$ (Li et al., 2008). The calculated $n(0)$ values are 2.39, 2.44, and 2.58 for CaZn₂N₂, SrZn₂N₂, and BaZn₂N₂, respectively. The static value of $k(0)$ is close to zero in the low photon energy region (0–2 eV). The static values of $R(0)$ are 0.168 for CaZn₂N₂, 0.175 for SrZn₂N₂, and 0.194 for BaZn₂N₂, respectively. The value of $R(\omega)$ always fluctuates between 0.15 and 0.35 in the range of 0–10 eV. It is observed from Fig. 7(f) that the absorption edge is mostly located at about 2 eV, which is linked with the band gap calculated by the direct electronic transition from the top of the valence band to the bottom of the conduction band. In the low photon energy range (0–2 eV), the absorption is negligible. Three compounds show the high light absorption properties. Especially, the efficiency of light absorption is greatly enhanced for BaZn₂N₂ in the visible and ultraviolet regions (2–5 eV), which is very conducive to improve the optical performance.

4. Conclusions

In summary, the structure, stability, elastic, electronic, and optical properties of trigonal AZn₂N₂ (A = Ca, Sr, Ba) are revealed for the first time in the current work. The stability and optoelectronic properties of BaZn₂N₂ are highlighted. The results show that three compounds are thermodynamically and mechanically stable, and they are brittle materials. Moreover, the stability of BaZn₂N₂ is further verified by applying different theoretical approaches. The direct band gap transition at the Γ point is allowed for each compound. The calculated direct band gaps are 1.733, 1.507, and 1.510 eV for CaZn₂N₂, SrZn₂N₂, and BaZn₂N₂, respectively. For three compounds, the electron exhibits high mobility for carrier transport, and the value of E_b is less than 80 meV. Detailed analysis of optical properties displays that BaZn₂N₂ has excellent light absorption capacity in the visible region. This findings reveal that BaZn₂N₂ is a good candidate for optoelectronic applications.

CRediT authorship contribution statement

Diwen Liu: Conceptualization, Supervision, Validation, Writing – original draft. **Huan Peng:** Formal analysis. **Rongjian Sa:** Resources, Writing – review & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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